¹ Formal specification of the Cardano blockchain

² ledger, mechanized in Agda

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8 — Abstract -

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- Blockchain systems comprise critical software that handle substantial monetary funds, rendering
 them excellent candidates for *formal verification*. One of their core components is the underlying
 ledger that does all the accounting: keeping track of transactions and their validity, etc.
- ¹² Unfortunately, previous theoretical studies are typically confined to an idealized setting, while ¹³ specifications for real implementations are scarce; either the functionality is directly implemented ¹⁴ without a proper specification, or at best an informal specification is written on paper.
- The present work expands beyond prior meta-theoretical investigations of the EUTxO model to encompass the full scale of the Cardano blockchain: our formal specification describes a hierarchy of modular transitions that covers all the intricacies of a realistic blockchain, such as fully expressive smart contracts and decentralized governance.
- It is mechanized in a proof assistant, thus enjoys a higher standard of rigor: type-checking prevents minor oversights that were frequent in previous informal approaches; key meta-theoretical properties can now be formally proven; it is an *executable* specification against which the implementation in production is being tested for conformance; and it provides firm foundations for smart contract verification.

Apart from a safety net to keep us in check, the formalization also provides a guideline for the ledger design: one informs the other in a symbiotic way, especially in the case of state-of-the-art features like decentralized governance, which is an emerging sub-field of blockchain research that however mandates a more exploratory approach.

All the results presented in this paper have been mechanized in the Agda proof assistant and are publicly available. In fact, this document is itself a literate Agda script and all rendered code has been successfully type-checked.

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1 Introduction

- This paper gives a high-level overview of the Cardano ledger specification in the Agda proof assistant, which is one of three core pieces of the Cardano blockchain:
- ³⁸ **Networking**: deals with sending messages across the internet.
- ³⁹ **Consensus**: establishes a common order of valid blocks.
- 40 **Ledger**: decides whether a sequence of blocks is valid.
- ⁴¹ Such *separation of concerns* is crucial to enable a rigidly formal study of each individual
- 42 component; the ledger is based on the *Extended UTxO* model (EUTxO), an extension of

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Bitcoin's model of unspent transaction outputs [19] – in contrast to Ethereum's account-based 43 model [8] – to accommodate fully expressive *smart contracts* that run on the blockchain. 44 Luckily for us, EUTxO enjoys a well-studied meta-theory [9, 10] that is also mechanized 45 in Agda, albeit in a much simpler setting where a single ledger feature is considered at a 46 time, but not how multiple concurrent features interact. We take this to the next level by 47 scaling up these prior theoretical results to match the complexity of the real world: the 48 Cardano blockchain being one of the top ten cryptocurrencies today by market capitalization, 49 it handles gigabytes of transactions that transfer hundred of millions US dollars, while 50 simultaneously supporting all these features plus many more that have not been formally 51 studied before. 52

We are happy to report that the formalization overhead has proven minuscule compared 53 to the development effort of the actual implementation, measured either by lines of code (~10 54 thousand lines of Agda formalization versus ~200 thousand of Haskell implementation) or 55 by number of man hours put in so far (only a couple of full-time formal methods engineers 56 versus tens of production developers). The result is a mechanized document that leaves little 57 room for error, additionally proves crucial invariants of the overall system , e.g., that the 58 global value carried by the system stays constant, formally stated in Section 4. It doubles as 59 an executable reference implementation that we can utilize in production for conformance 60 testing. All of our work, much like this paper, is mechanized in Agda and is publicly available: 61

62

https://github.com/IntersectMBO/formal-ledger-specifications

Scope. Cardano's evolution proceeds in *eras*, each introducing a new vital feature to the 63 previous ones. While we would ideally want to provide a multitude of formal artifacts, each 64 describing a single era in full detail, the specification formalized here is that of the Voltaire 65 era that introduces decentralized governance as described in the Cardano Improvement 66 Proposal (CIP) 1694.¹ This stems from the fact that the design of the blockchain happens in 67 tandem with the formal specification; one informs the other in an intricate, non-linear fashion. 68 Thus arises a pragmatic need to think of the process as an act of balance between keeping 69 up with the *past*, *i.e.*, going back to previous eras and incrementally incorporating their 70 features, and co-evolving with the current design of the *future* ledger capabilities. Therefore, 71 we set aside details of the previous Byron, Shelley, and Alonzo eras while at the same 72 time missing orthogonal features related to smart contracts brought in the **Babbage** era. 73

Transitions as relations. The ledger can itself be conceptually divided into multiple 74 sub-components, each described by a transition between states that only contains the relevant 75 parts of the overarching ledger state and possibly some internal auxiliary information that is 76 discarded at the outer layer. These transitions are not independent, but form a hierarchy 77 of "state machines" where some higher-level transition might demand successful transition 78 of a sub-component down the dependency graph as one of its premises. Eventually, these 79 cascading transitions all get combined to dictate the top-level transition that handles an 80 individual block of transactions submitted to the blockchain. 81

Formally, we formulate such (labeled) transitions as relations X between the environment Γ inherited from a higher layer, an initial state s, a signal b that acts as user input, and a final state s':

		Environments	
85	$\Gamma \vdash s \xrightarrow{b}_X s'$	(Signals)	States
		Possible	transitions

¹ https://github.com/cardano-foundation/CIPs/blob/17771640/CIP-1694/README.md

We will henceforth present such transitions as shown on the right; a *triptych* defining 86 environments and possibly signals (top left), states (top right), and the rules that *inductively* 87 define the transition (bottom). 88

1.1 Agda preliminaries 89

In Agda, the aforementioned ledger transitions are modeled as *inductive families* of type: 90

91

 $_\vdash_ \rightharpoonup (_)_ : Env \rightarrow State \rightarrow Signal \rightarrow State \rightarrow \mathsf{Type}$

Reflexive transitive closure. We will often need to apply a transition repeatedly until 92 we arrive at a final state, which corresponds to the standard mathematical construction of 93 taking the relation's *reflexive transitive closure*: 94

data $_\vdash_ \rightharpoonup (]_) *_ : Env \rightarrow State \rightarrow \mathsf{List} Signal \rightarrow State \rightarrow \mathsf{Type}$ where 95

			step :	
	base	:	• $\Gamma \vdash s \rightharpoonup (b$) s'
96			• $\Gamma \vdash s' \rightharpoonup (bs$)* <i>s</i> "
97		$\Gamma \vdash s \rightharpoonup ([]) * s$	$\Gamma \vdash s \rightharpoonup (b::b)$	os)* s"

9

One particular trait we inherited from previous pen-and-paper 98 Finite sets & maps. iterations of the ledger specification is a heavy use of set theory, which goes against Agda's 99 foundations in Type Theory, both technically and in a philosophical sense. To remedy this, 100 we have developed an in-house library for conducting Axiomatic Set Theory within the type-101 theoretic setting of Agda [18]; we stay in its finite fragment for this application. Crucially, the 102 type of sets is entirely *abstract*: there is no way to utilize proof-by-computation (e.g., as one 103 would do when modeling sets as lists of distinct elements), so that all proofs eventually resort 104 to the axioms and the library's implementation details stay irrelevant. At the same time, 105 when extracting executable code the library provides a properly executable implementation-106 the abstraction layer only exists at compile-time. Implementing this abstraction layer helped 107 us greatly reduce code complexity and size over a previous list-based approach. In fact, it is 108 highly encouraged to provide *multiple* implementations without affecting the formalization 109 and the validity of the established proofs therein. 110

Equipped with the axioms provided by the library, e.g., the ability to construct power 111 sets \mathbb{P} , it is remarkably easy to define common set-theoretic concepts like set inclusion and 112 extensional equality of sets (left), as well as re-purpose sets of key-value pairs to model *finite* 113 $maps^2$ by imposing uniqueness of keys (right): 114

-

115

2

$$\begin{array}{c} \underline{\subseteq} \\ & \subseteq \\ X \subseteq \\ Y = \forall \\ \{x\} \rightarrow x \in \\ X \rightarrow x \in \\ Y \rightarrow x \in \\ X \rightarrow x \in \\ Y \rightarrow x \in \\ X \rightarrow x \in \\ Y \rightarrow x \in \\ Y \rightarrow x \in \\ Y \rightarrow \\ X \rightarrow \\ Y = \\ X = \\ Y = \\ X \subseteq \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y \rightarrow \\ Y = \\ X = \\ Y \rightarrow \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y \rightarrow \\ Y \rightarrow \\ Y = \\ Y \rightarrow \\ Y \rightarrow$$

It is natural to think of maps as partial functions, but unrestricted Agda functions would not do here.

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¹¹⁶ **2** Fundamental entities

117 2.1 Cryptographic primitives

There are two types of credentials that can be used on Cardano: VKey and script credentials. VKey credentials use a public key signing scheme (Ed25519) for verification. Some serialized (Ser) data can be signed, and isSigned is the property that a public VKey signed some data with a given signature (Sig). There are also other cryptographic primitives in the Cardano ledger, for example KES and VRF used in the consensus layer, but we omit those here.

Script credentials correspond to a hash of a script that has to be executed by the ledger as part of transaction validation. There are two different types of scripts, native and Plutus, but the details of this are not relevant for the rest of this paper.

 $\label{eq:lissing} {\sf 126} \qquad {\sf VKey Sig Ser: Type} \qquad {\sf isSigned: VKey } \rightarrow {\sf Ser} \rightarrow {\sf Sig} \rightarrow {\sf Type}$

In the specification, all definitions that require these primitives must accept these as 127 additional arguments. To streamline this process, these definitions are bundled into a record 128 and, using Agda's module system, are quantified only once per file. We are using this pattern 129 many times, either to introduce additional abstraction barriers or to effectively provide 130 foreign functions within a safe environment. Additionally, particularly fundamental interfaces 131 like the one presented above are sometimes re-bundled transitively into larger records, which 132 further streamlines the interface. This is in stark contrast to the Haskell implementation, 133 which often needs to repeat tens of type class constraints on many functions in a module. 134

135 2.2 Addresses

There are various types of addresses used for storing funds in the UTxO set, which all contain a payment Credential and optionally a staking Credential. Addr is the union of all of those types. A Credential is a hash of a public key or script, types for which are kept abstract. The most common type of address is a BaseAddr which must include a staking Credential.

There is also a special type of address (not included in Addr) without a payment credential, called a reward address. It is not used for interacting with the UTxO set, but instead used to refer to reward accounts [31].

143 $Credential = KeyHash \uplus ScriptHash$

record BaseAddr : Type where	record RwdAddr : Type where
pay : Credential	stake : Credential
stake : Credential	Stake . Credential

 $_{145} \quad \mathsf{Addr} = \mathsf{BaseAddr} \uplus \dots$

144

146 **2.3 Base types**

The basic units of currency and time are Coin, Slot and Epoch, which we treat as natural numbers, while an implementation might use isomorphic but more complicated types (for example to represent the beginning of time in a special way).

150 $Coin = Slot = Epoch = \mathbb{N}$

¹⁵¹ A Coin is the smallest unit of currency, a Slot is the smallest unit of time (corresponding to 1 ¹⁵² second in the main chain), and an Epoch is a fixed number of slots (corresponding to 5 days in the main chain). Every slot, a stake pool has a random chance to be able to mint a block,
and one block every five slots is expected [13].

3 Advancing the blockchain

156 3.1 Protocol parameters

We start with adjustable protocol parameters. In contrast to constants such as the length of
an Epoch, these parameters can be changed while the system is running via the governance
mechanism. They can affect various features of the system, such as minimum fees, maximum
and minimum sizes of certain components, and more.

The full specification contains well over 20 parameters, while we only list a few. The maximum sizes should be self-explanatory, while a and b are the coefficients of a polynomial used in the calculation of the minimum fee for transactions (*c.f.*, function minfee in Appendix B).

```
    record PParams : Type where
    maxBlockSize maxTxSize a b : N
```

3.2 Extending the blockchain block-by-block

CHAIN is the main state machine describing the ledger. Since it is not invoked from any 168 other state machine, it does not have an environment. It invokes two other state machines, 169 NEWEPOCH and LEDGER^{*}, where the former detects if the new block b is in a new epoch. 170 In that case, NEWEPOCH takes care of various bookkeeping tasks, such as counting votes for 171 the governance system and updating stake distributions for consensus. For a basic version 172 that detects whether a new epoch has been entered, see Appendix C. The potentially updated 173 state is then given to LEDGER*, which is the reflexive-transitive closure of LEDGER and 174 applies all the transactions in the block in sequence. Finally, CHAIN updates ChainState with 175 the resulting states. 176

There is a key property about NEWEPOCH, which is that it never gets stuck, i.e. that for all states, environments and signals it always transitions to a new state. This property is proven in our development.

	record NewEpochState : Type where lastEpoch : Epoch
	acnt : Acnt
record Block : Type where	ls : LState
ts : List Tx	es : EnactState
slot : Slot	fut : RatifyState
	record ChainState : Type where
	newEpochState : NewEpochState

181 CHAIN :

• mkNewEpochEnv $s \vdash s$.newEpochState $\rightarrow ($ epoch slot ,NEWEPOCH) nes

- [slot \otimes constitution .proj₁ .proj₂ \otimes pparams .proj₁ \otimes es $]] \vdash$ nes .ls \rightarrow (ts ,LEDGER*) ls '
- 184 185

182

 $_ \vdash s \rightharpoonup (b, \mathsf{CHAIN})$ updateChainState $s \ nes$

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3.3 Extending the ledger transaction-by-transaction 186

Transaction processing is broken down into three separate parts: accounting & witnessing 187 (UTXOW), application of certificates (CERT) and processing of governance votes & proposals 188 (GOV).189

record LEnv : Type where slot : Slot ppolicy : Maybe ScriptHash pparams : PParams enactState : EnactState	record LState : Type where utxoSt : UTxOState govSt : GovState certState : CertState
---	---

LEDGER : 191 • mkUTxOEnv $\Gamma \vdash$ utxoSt \rightharpoonup (*tx*,UTXOW) *utxoSt'* 192 • [] epoch slot ⊗ pparams ⊗ txvote ⊗ txwdrls]] ⊢ certState →(| txcerts ,CERT*)) certState ' 193 • \llbracket txid \otimes epoch slot \otimes pparams \otimes enactState $\rrbracket \vdash$ govSt \rightharpoonup (txgov *txb* ,GOV*) *govSt'* 194 195 $\Gamma \vdash s \rightharpoonup (tx, \mathsf{LEDGER}) [utxoSt' \otimes govSt' \otimes certState']]$ 196

(The notation $[\ldots \otimes \ldots]$ constructs records of any type by giving their fields in order.) 197

UT_xO 4 198

Witnessing 4.1 199

Transaction witnessing checks that all required signatures are present and all required scripts 200 accept the validity of the given transaction. witsKeyHashes and witsScriptHashes is the set 201 of hashes of keys/scripts included in the transaction. 202

```
UTXOW-inductive :
203
          • witsVKeyNeeded ppolicy utxo txb \subseteq witsKeyHashes
204
          • scriptsNeeded ppolicy utxo txb \equiv witsScriptHashes
205
          • \forall [(vk, \sigma) \in vkSigs] isSigned vk (txidBytes txid) \sigma
206
          • \forall [s \in \text{scriptsP1}] validP1Script witsKeyHashes txvldt s
207
          • \Gamma \vdash s \rightharpoonup (tx, \mathsf{UTXO}) s'
208
209
             \Gamma \vdash s \rightharpoonup (tx, \mathsf{UTXOW}) s'
```

```
4.2
         Accounting
211
```

210

Accounting is handled by the UTXO state machine. The preconditions for UTXO-inductive 212 ensure various properties or prevent attacks. For example, if txins was allowed to be empty, 213 one could make a transaction that only spends from reward accounts. This does not require a 214 specific hash to be present in the transaction body, so such a transaction could be repeatable in 215 certain scenarios. The equation between produced and consumed ensures that the transaction 216 is properly balanced. For details on some of these functions, see Appendix B. 217

218	record UTxOEnv : Type where slot : Slot pparams : PParams Deposits = DepositPurpose → Coin	record UTxOState : Type where utxo : UTxO deposits : Deposits fees donations : Coin	
219	UTXO-inductive :		
220	• txins $\neq \varnothing$		
221	• txins \subseteq dom utxo		
222	• minfee pp $tx \leq txfee$		
223	• txsize \leq maxTxSize pp		
224	• consumed pp $s \text{ txb} \equiv \text{produced pp } s \text{ txb}$		
225	• coin mint $\equiv 0$		
226			
	[(utxo txins) U	J outs txb	
	\otimes updateDeposite	; pp txb deposits	
227	$\Gamma dash s riangleq (\!\! tx \ , UTXO)\!\!) \ \otimes fees + txfee$		
	\otimes donations + tx	donation]	

Property 4.1 (Value preservation).

Let getCoin be the sum of all coins contained within a UTxOState. Then, for all $\Gamma \in UTxOEnv$, s, s' $\in UTxOState$ and $tx \in Tx$, if tx .body .txid \notin map proj₁ (dom (s .UTxOState.utxo))and Γ s $\rightarrow (tx, UTXO)$ s'then getCoin $s \equiv$ getCoin s'.

Note that this is one of the most important properties of a UTxO-based ledger, as evidenced by its central place in EUTxO's meta-theory [9, 10].

5 Decentralized Governance

235 5.1 Entities and actions

The governance framework has three bodies of governance, the constitutional committee, delegated representatives and stake pool operators, corresponding to the roles CC, DRep and SPO. Proposals relevant to the governance system come in the form of Governance Actions. They are identified by their GovActionID, which consists of the Txld belonging to the transaction that proposed it and the index within that transaction (a transaction can propose multiple governance actions at once).

242	$GovActionID = TxId \times \mathbb{N}$	
243	data GovRole : Type where	
244	CC DRep SPO : GovRole	
245	data GovAction : Type where	
246	NoConfidence :	GovAction
247	$NewCommittee \hspace{0.1 in}:\hspace{0.1 in} Credential \rightharpoonup Epoch \rightarrow \mathbb{P} \hspace{0.1 in} Credential \rightarrow \mathbb{Q} \rightarrow \mathbb{P}$	GovAction
248	$NewConstitution : DocHash \to Maybe \; ScriptHash \qquad \to $	GovAction
249	TriggerHF : ProtVer \rightarrow	GovAction
250	$ChangePParams \ : \ PParamsUpdate \qquad \qquad \rightarrow \qquad $	GovAction
251	$TreasuryWdrl : (RwdAddr \rightharpoonup Coin) \qquad \qquad \rightarrow$	GovAction
252	Info :	GovAction

²⁵³ For the meaning of these individual actions, see [12].

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5.2 Votes and proposals

Before a Vote can be cast it must be packaged together with further information, such as who is voting and for which governance action. This information is combined in the GovVote record. To propose a governance action, a GovProposal needs to be submitted. Beside the

 $_{\tt 258}$ $\,$ proposed action, it requires a deposit, which will be returned to <code>returnAddr</code>.

data Vote : Type where yes no abstain : Vote	record GovVote : Type where gid : GovActionID role : GovRole credential : Credential vote : Vote	record GovProposal : Type where action : GovAction deposit : Coin returnAddr : RwdAddr
---	--	---

260 5.3 Enactment

Enactment of a governance action is carried out via the ENACT state machine. We just show two example rules for this state machine—there is one corresponding to each constructor of

²⁶³ GovAction. For an explanation of the hash protection scheme, see Appendix A.

		record EnactState : Type where
	record EnactEnv : Type where	cc : HashProtected (Maybe ((Credential \rightarrow Epoch) \times Q))
264	gid : GovActionID	constitution : HashProtected (DocHash $ imes$ Maybe ScriptHash)
	treasury : Coin	pv : HashProtected ProtVer
	epoch : Epoch	pparams : HashProtected PParams
		withdrawals : RwdAddr → Coin

Enact-NewConst : $\begin{bmatrix} gid \otimes t \otimes e \end{bmatrix} \vdash s \rightharpoonup (NewConstitution \ dh \ sh \ ,ENACT) \ record \ s \ \{ \ constitution = (dh \ , sh) \ , \ gid \ \}$ Enact-Wdrl : $\begin{bmatrix} let \ newWdrls = s \ .withdrawals \cup \ wdrl \ in \ \sum [\ x \leftarrow \ newWdrls \] \ x \le t$ $\begin{bmatrix} gid \otimes t \otimes e \end{bmatrix} \vdash s \rightharpoonup (\ TreasuryWdrl \ wdrl \ ,ENACT) \ record \ s \ \{ \ withdrawals = \ newWdrls \ \}$

²⁷³ (The record keyword indicates a record update, i.e. we take the existing EnactState and ²⁷⁴ update one of its fields.)

275 5.4 Voting and Proposing

The order of proposals is maintained by keeping governance actions in a list—this acts as a tie breaker when multiple competing actions might be able to be ratified at the same time. 278

votes: (GovRole × Credential) → VotereturnAddr: RwdAddrexpiresIn: Epochaction: GovActionprevAction: NeedsHash action	record GovEnv : Type whe txid : Txld epoch : Epoch pparams : PParams enactState : EnactState
--	--

GOV-Vote : 279 • $(aid, ast) \in fromList s$ 280 • canVote pparams (action *ast*) role 281 282 $(\Gamma, k) \vdash s \rightharpoonup (sig, GOV)$ addVote s aid role cred v 283 284 GOV-Propose : 285 • actionWellFormed $a \equiv true$ 286 • $d \equiv govActionDeposit$ 287 288 $(\Gamma, k) \vdash s \rightarrow (inj_2 \ prop \ , GOV)$ addAction s (govActionLifetime + epoch) (txid , k) addr a prev 289

290 5.5 Ratification

Governance actions are *ratified* through on-chain voting actions. Different kinds of governance actions have different ratification requirements but always involve at least *two of the three* governance bodies. The voting power of the DRep and SPO roles is proportional to the stake delegated to them, while the constitutional committee has individually elected members where each member has the same voting power.

Some actions take priority over others and, when enacted, delay all further ratification to the next epoch boundary. This allows a changed government to reevaluate existing proposals.

	record RatifyEnv : Type where	record RatifyState : Type where
	stakeDistrs : StakeDistrs	es : EnactState
298	currentEpoch : Epoch	$removed : \mathbb{P} \; (GovActionID \times GovActionState)$
	$\frac{dreps}{redential} \rightarrow Epoch$	delay : Bool

RATIFY-Accept : 299 • accepted Γ es st 300 • \neg delayed action prevAction es d301 • $[a : proj_1 \otimes treasury \otimes currentEpoch] \vdash es \rightarrow (action, ENACT) es'$ 302 303 $]\!] \rightharpoonup (\![a], \mathsf{RATIFY}])$ $\Gamma \vdash \llbracket es \otimes removed$ $\otimes d$ 304 $[es' \otimes \{a\} \cup removed \otimes delayingAction action]$ 305 306 **RATIFY-Reject** : 307 • \neg accepted Γ es st 308 • expired currentEpoch st 309

```
\Gamma \vdash \llbracket es \otimes removed \otimes d \rrbracket \rightharpoonup (\llbracket a, \mathsf{RATIFY}) \rrbracket es \otimes \{\llbracket a \} \cup removed \otimes d \rrbracket
311
312
         RATIFY-Continue :
313
                 (• \neg accepted \Gamma es st • \neg expired currentEpoch st)
314
             315
                    • ( delayed action prevAction es d
316

\exists (\forall es' \rightarrow \neg [] a .proj_1 \otimes treasury \otimes currentEpoch ]] \vdash es \rightarrow (|| action , ENACT |) es')))

317
318
                 \Gamma \vdash \llbracket es \otimes removed \otimes d \rrbracket \rightharpoonup \llbracket a , \mathsf{RATIFY} \rrbracket \llbracket es \otimes removed \otimes d \rrbracket
319
```

³²⁰ The main new ingredients for the rules of the RATIFY state machine are:

- accepted, which is the property that there are sufficient votes from the required bodies to pass this action;
- ³²³ delayed, which expresses whether an action is delayed;
- ³²⁴ expired, which becomes true a certain number of epochs after the action has been proposed.

The three RATIFY rules correspond to the cases where an action can be ratified and enacted (in which case it is), or it is expired and can be removed, or, otherwise it will be kept around for the future. This means that all governance actions eventually either get accepted and enacted via RATIFY-Accept or rejected via RATIFY-Reject. It is not possible to remove actions by voting against them, one has to wait for the action to expire.

6 Transactions

310

³³¹ A transaction is made up of a transaction body and a collection of witnesses.

	record TxBody : Type where	record TxWitnesses : Type where
	txins : ℙ TxIn	vkSigs ∶ VKey → Sig
	$txouts : Ix \rightharpoonup TxOut$	scripts : ℙ Script
	txfee : Coin	
336	txvote : List GovVote	
	txprop : List GovProposal	record Tx : Type where
	txsize : ℕ	body : TxBody
	txid : Txld	wits : TxWitnesses

- 337 Some key ingredients in the transaction body are:
- A set of transaction inputs (txins), each of which identifies an output from a previous transaction. A transaction input (Txln) consists of a transaction ID and an index to uniquely identify the output.
- ³⁴¹ An indexed collection of transaction outputs (txouts). A transaction output (TxOut) is ³⁴² an address paired with a multi-asset Value (see [10]).
- A transaction fee (txfee), whose value will be added to the fee pot.

The size (txsize) and the hash (txid) of the serialized form of the transaction that was included in the block. Cardano's serialization is not canonical, so any information that is necessary but lost during descrialisation must be preserved by attaching it to the data like this.

348

7 Compiling to a Haskell implementation & Conformance testing

³⁴⁹ In order to deliver on our promise that the specification is also *executable*, there is still some ³⁵⁰ work to be done given that all transitions have been formulated as relations.

This is precisely the reason we also manually prove that each and every transition of the previous sections is indeed *computational*:

The definition above captures what it means for a (small-step) relation to be accurately computed by a function compute, which given as input an environment, source state, and signal, outputs the resulting state or an error for invalid transitions. Most importantly, such a function must be *sound* and *complete*: it does not return output states that are not related, and, *vice versa*, all related states are successfully returned. An alternative interpretation is that this rules out *non-determinism* across all ledger transitions, *i.e.*, there cannot be two distinct states arising from the same inputs.

There is one last obstacle that hinders execution: we have leveraged Agda's module system³ to parameterize our specification over some abstract types and functions that we assume as given, *e.g.*, the cryptographic primitives. As a final step, we instantiate these parameters with concrete definitions, either by manually providing them within Agda, or deferring to the Haskell *foreign function interface* to reuse existing Haskell ones that have no Agda counterpart.

Equipped with a fully concrete specification and the Computational proofs for each relation, 369 it is finally possible to generate executable Haskell code using Agda's MAlonzo compilation 370 backend.⁴ The resulting Haskell library is then deployed as part of the automated testing 371 setup for the Cardano ledger in production, so as to ensure the developers have faithfully 372 implemented the specification. This is made possible by virtue of the implementation 373 mirroring the specification's structure to define transitions, which one can then test by 374 randomly generating environments/states/signals, and executing both state machines on 375 these same random inputs to compare the final results for *conformance*. 376

One small caveat remains though: production code might use different data structures, mainly for reasons of *performance*, which are not isomorphic to those used in the specification and might require non-trivial translation functions and notions of equality to perform the aforementioned tests. In the future, we plan to also formalize these more efficient representations in Agda and prove that soundness is preserved regardless.

382 8 Related Work

383 **EUTxO.** The approach we followed is a natural evolution of prior meta-theoretical results

³ https://agda.readthedocs.io/en/v2.6.4/language/module-system.html#parameterised-modules

⁴ https://agda.readthedocs.io/en/v2.6.4/tools/compilers.html#ghc-backend

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³⁸⁴ on the EUTxO model [9, 10], but now employed at a much larger scale to cover all the ³⁸⁵ features of a realistic ledger: epochs, protocol parameters, decentralized governance, *etc.*

All this complexity does not come for free though: one has to be economical about which properties to prove of the resulting system, and this might entail limiting oneself to mechanizing just the core properties, such as global value preservation as we saw with Property 4.1, otherwise the whole effort can quickly become practically infeasible to maintain from a software-engineering perspective.

Formal Methods, generally. The overarching methodology—formally specifying the system under design—is by no means particular to the blockchain space. A principal success story in the wider computing world nowadays is definitely the *WebAssembly* language, an alternative to Javascript to act as a compilation target for web applications with performance and security in mind [16], which was designed in tandem with a formalization of its semantics [29].

Apart from keeping programming language designers honest by making sure no edge cases are overlooked, it allows the language to evolve in a much more robust fashion: every future extension has to pass through a rigorous process which eventually involves extending the formalization itself.

While the WebAssembly line of work [29, 30] provided much inspiration for us, we believe our approach to be even more radical by mitigating the need for informal processes altogether: the formalization *is* the specification!

Formal Methods, specifically for blockchain. The work presented here fits well within Cardano's vision for *agile formal methods* [17], which strikes a good balance between a fully certified implementation (too much effort, too few resources) and an informal, under-specified product (quicker, easier, but far less trustworthy). Instead of demanding the impossible by extracting the actual production from the formalization itself, we find the sweet spot lies in the middle: extracting a *reference implementation* in Haskell and using *conformance testing* to ensure the system in production behaves as it should (*c.f.*, Section 7).

Apart from our work, there are very few mechanized results on UTxO-based blockchains (modeled after Bitcoin [19]), and all of them invariably are formulated on a idealized setting [26, 1, 9, 10], abstracting away the complexity that ensues when multiple features interact. Thus, the mechanized specification presented here for the Cardano ledger is the first of its kind, and we hope this sets a higher standard for subsequent work and pushes forward a more formal agenda for blockchain research in the future.

Although not directly comparable to our use case, account-based blockchains (modeled 417 after Ethereum [8]) fair better in this respect, with plenty of formal method tools available, 418 ranging from model checking [15, 28] to full-blown formal verification [11, 7, 23]. Notable 419 blockchains that spearhead progress in this direction include Tezos [5, 6, 14], Ziliiqa and its 420 Scilla smart-contract language [25, 24], and Concordium [3, 21, 2, 27, 20]. The main difference 421 with our work lies in *readability*, partly due to the choice of tool (Agda being notorious for 422 its beautiful renderings but lack of proper support for practical "big" proofs that arise in 423 large scale software verification projects, where tactic-based proof assistants like Coq [4] 424 and Isabelle [22] are more common), and the point where mechanization is placed within 425 the development pipeline: most aforementioned work builds upon informal pen-and-paper 426 documents and some of its aspects are only mechanized *a-posteriori*. Having said that, 427 the fundamental split stems from a completely different *target audience*; our formalization 428 is meant to be read by researchers, formal methods engineers, compiler engineers, and 429 developers alike. In contrast, the majority of the aforementioned work is primarily targeted 430 at a select team of experts which complement other (informal) documentation and software. 431

432 9 Conclusion

⁴³³ We have outlined the mechanized specification of the EUTxO-based ledger rules of the ⁴³⁴ Cardano blockchain, by taking a *bird's-eye view* of the hierarchy of transitions handling ⁴³⁵ different sub-components in a modular way.

Although space limitations preclude us from exhaustively fleshing out all the gory details 436 of our formalization, we hope to have conveyed the general design principles that will be 437 helpful to others when attempting to mechanize something of this kind and at this scale. 438 In the little space we could afford for more thorough details, we made a conscious choice 439 of putting emphasis on the most novel aspect of the current era of the Cardano blockchain: 440 decentralized governance. There, the introduction of the notions of voting, ratification, and 441 enactment complicate the ledger rules of previous eras—albeit in a fairly orthogonal way, 442 which we found particularly satisfying. 443

A mechanized formal artifact of this kind is rigid enough to eliminate any ambiguity that would often arise in pen-and-paper specifications, all the while sustaining a readable document that is accessible to a wide audience and allows for varied uses.

By virtue of conducting our work within a proof assistant based on *constructive* logic, our result extends beyond a purely theoretical exercise to an *executable* resource that can be leveraged as a *reference implementation*, against which a system-in-production can be tested for conformance.

Last but not least, it is evident that developing a ledger on these foundations opens up a plethora of opportunities for further formalization work, *e.g.*, instantiating the abstract notion of scripts with actual *Plutus* scripts brings us close to enabling practical smart contract verification where developers write their programs immediately in Agda, prove properties about their behavior, and then extract Plutus code they can deploy to the actual Cardano blockchain. All these point to bright prospects for formal methods in UTxO-based blockchains, which we are excited to explore in the future and hope that others do as well.

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A Governance helper calculations

The design of the hash protection mechanism is elaborated here. The issue at hand is that different actions of the same type may override each other, and they allow for partial modifications to the state. So if arbitrary actions were allowed to be applied, the system may end up in a particular state that was never intended and voted for.

In the original design of the governance system, the fix for this issue was to allow only a single governance action of each type to be enacted per epoch. This restriction is a potentially severe limitation and may open the door to some types of attacks.

The final design instead requires some types of governance actions to reference the ID of the parent they are building on, similar to a Merkle tree. Then, in a single epoch the system can take arbitrarily many steps down that tree, and since IDs are unforgeable, the system is only ever in a state that was publically known prior to voting.

There are two governance actions where this mechanism is not required, because they either commute naturally or they do not actually affect the state. For these it is more convenient to not enforce dependencies.

```
NeedsHash : GovAction \rightarrow Type
606
607
      NeedsHash NoConfidence
                                              = GovActionID
      NeedsHash (NewCommittee _ _ _) = GovActionID
608
      NeedsHash (NewConstitution _ _) = GovActionID
609
      NeedsHash (TriggerHF _)
                                              = GovActionID
610
      NeedsHash (ChangePParams _)
                                              = GovActionID
611
      NeedsHash (TreasuryWdrl _)
                                              = T
612
      NeedsHash Info
                                              = T
613
614
      HashProtected : Type \rightarrow Type
615
      HashProtected A = A \times \text{GovActionID}
616
617
         The two functions adjusting the state in GOV are addVote and addAction.
618
         addVote inserts (and potentially overrides) a vote made for a particular governance action
619
     by a credential in a role.
620
         addAction adds a new proposed action at the end of a given GovState, properly initializing
621
     all the requiered fields.
622
      \mathsf{addVote}:\,\mathsf{GovState}\to\mathsf{GovActionID}\to\mathsf{GovRole}\to\mathsf{Credential}\to\mathsf{Vote}\to\mathsf{GovState}
623
      addVote s aid r kh v = map modifyVotes s
624
        where modifyVotes =\lambda~(gid , s')
ightarrow gid , record s'
625
                  { votes = if gid \equiv aid then insert (votes s') (r, kh) v else votes s'}
626
627
      addAction : GovState
628
                  \rightarrow Epoch \rightarrow GovActionID \rightarrow RwdAddr \rightarrow (a : GovAction) \rightarrow NeedsHash a
629
                  \rightarrow GovState
630
      addAction s \ e \ aid \ addr \ a \ prev = s :: (aid , record)
631
         { votes = \emptyset ; returnAddr = addr ; expiresIn = e ; action = a ; prevAction = prev })
632
```

633

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634 B UTxO

⁶³⁵ Some of the functions used to define the UTXO and UTXOW state machines are defined here; ⁶³⁶ inject is the function takes a Coin and turns it into a multi-asset Value [10].

```
outs : TxBody \rightarrow UTxO
637
       outs tx = mapKeys (tx .txid , _) (tx .txouts)
638
639
       \mathsf{minfee}:\,\mathsf{PParams}\to\mathsf{Tx}\to\mathsf{Coin}
640
       minfee pp \ tx = pp .a * tx .body .txsize + pp .b
641
642
       consumed : PParams \rightarrow UTxOState \rightarrow TxBody \rightarrow Value
643
       consumed pp st txb
644
          = balance (st .utxo | txb .txins)
645
          + txb .mint
646
          + inject (depositRefunds pp st txb)
647
648
       produced : PParams \rightarrow UTxOState \rightarrow TxBody \rightarrow Value
649
       produced pp \ st \ txb
650
          = balance (outs txb)
651
          + inject (txb .txfee)
652
          + inject (newDeposits pp \ st \ txb)
653
          + inject (txb .txdonation)
654
655
       credsNeeded : Maybe ScriptHash \rightarrow UTxO \rightarrow TxBody \rightarrow \mathbb{P} (ScriptPurpose \times Credential)
656
       credsNeeded p utxo txb
657
          = map (\lambda (i, o) \rightarrow (Spend i, payCred (proj<sub>1</sub> o))) ((utxo \mid txins) )
658
          \cup map (\lambda a \rightarrow (Rwrd a , RwdAddr.stake a)) (dom $ txwdrls .proj<sub>1</sub>)
659
          \cup map (\lambda \ c \rightarrow (Cert c , cwitness c)) (fromList txcerts)
660
          \cup map (\lambda x \rightarrow (Mint x, inj<sub>2</sub> x)) (policies mint)
661
          \cup map (\lambda v \rightarrow (Vote v, GovVote.credential v)) (fromList txvote)
662
          \cup (if p then (\lambda \{sh\} \rightarrow map \ (\lambda \ p \rightarrow (Propose \ p \ , inj_2 \ sh)) (fromList txprop))
663
                 else \emptyset)
664
          where open TxBody txb
665
666
       witsVKeyNeeded : Maybe ScriptHash \rightarrow UTxO \rightarrow TxBody \rightarrow \mathbb{P} KeyHash
667
       witsVKeyNeeded sh = mapPartial islnj_1 \circ_2 map proj_2 \circ_2 credsNeeded sh
668
669
       \mathsf{scriptsNeeded} \ : \ \mathsf{Maybe} \ \mathsf{ScriptHash} \ \to \ \mathsf{UTxO} \ \to \ \mathsf{TxBody} \ \to \ \mathbb{P} \ \mathsf{ScriptHash}
670
       scriptsNeeded sh = mapPartial islnj_2 \circ_2 map proj_2 \circ_2 credsNeeded <math>sh
671
672
```

673 C Advancing epochs

The NEWEPOCH state machine is responsible for detecting epoch changes: either the epoch remains unchanged (NEWEPOCH-Not-New), or the immediately next epoch is reached and the state is updated subject to some ratification requirements (NEWEPOCH-New).

```
NEWEPOCH-New :
677
              • e \equiv suc \ lastEpoch
678
              • record { currentEpoch = e ; treasury = treasury ; GState gState ; NewEpochEnv \Gamma }
679
                     \vdash [\![ \ es \,\otimes\, \varnothing \,\otimes\, {\sf false} \,]\!] \rightharpoonup (\![ \ govSt' \ , {\sf RATIFY}* \ )\!] \ fut'
680
681
                 \Gamma \vdash \mathit{nes} \rightharpoonup (\!\!| e \ , \mathsf{NEWEPOCH} \ ) [\!\!| e \otimes \mathit{acnt'} \otimes \mathit{ls'} \otimes \mathit{es} \otimes \mathit{fut'} \ ]\!\!]
682
683
         NEWEPOCH-Not-New :
684
              e \not\equiv \mathsf{suc} \ \mathsf{lastEpoch}
685
686
             \Gamma \vdash nes \rightharpoonup (e, NEWEPOCH) nes
687
```

688